

- You have up to 90 minutes.
- All questions are compulsory.
- Every item on the test awards 4 points for each correct answer and -1 for an incorrect answer.
- Calculators are allowed.

### Part I: Quantitative Aptitude

1. A and B participate in a race of 1 km. A beats B by 28 meters or 7 seconds. How much time does A take to complete the race?
  - (a) 4 minutes 3 seconds.
  - (b) 4 minutes 10 seconds.
  - (c) 3 minutes 57 seconds.
  - (d) 4 minutes 17 seconds.
2. How many terms are there in 3, 9, 27, 81,  $\dots$ , 531441?
  - (a) 10
  - (b) 11
  - (c) 12
  - (d) None of the above.
3. What is the missing number in 2, 5, 9, 19, 37, ....
  - (a) 73
  - (b) 74
  - (c) 75
  - (d) None of these.
4. A shopkeeper sells a product at a profit of 20%. If the selling price is \$480, what is the cost price of the product?
  - (a) \$400
  - (b) \$450
  - (c) \$500

- (d) \$600
5. A train travels at a speed of 60 km/hr for the first 30 minutes, then at a speed of 90 km/hr for the next 1 hour and 20 minutes, and finally at a speed of 40 km/hr for the last 45 minutes. What is the total distance covered by the train?
- (a) 90 km  
(b) 120 km  
(c) 180 km  
(d) 210 km
6. If some politicians are corrupt and all corrupt individuals are dishonest, which of the following statements is necessarily true?
- (a) All politicians are dishonest.  
(b) Some dishonest individuals are politicians.  
(c) All corrupt individuals are politicians.  
(d) Some politicians are honest.
7. If A is the brother of B, B is the sister of C, and C is the father of D, then how is A related to D?
- (a) Father  
(b) Brother  
(c) Uncle  
(d) None of the above
8. X and Y are two alloys of copper and iron prepared by mixing metals in the ratio 1:2 and 4:5, respectively. If equal quantities of alloys, e.g., X and Y, are melted to form a third alloy, Z, the ratio of copper to iron in Z is
- (a) 7:11  
(b) 5:7  
(c) 1:3  
(d) None of these
9. A shopkeeper purchased two varieties of rice: 200 KG at Rs. 20/KG and 100 KG at Rs. 50/KG. Being greedy, the shopkeeper mixed the two rice varieties and sold the mixture at a gain of 20%. Find the per KG selling price of the mixed rice.
- (a) 30  
(b) 32  
(c) 36

- (d) 40
10. The population of a city X, which is 1,00,000, decreases at 1500/year. The population of city Y, which is 50,000, increases at the rate of 1000/year. After how many years did the population of cities X and Y become equal?
- (a) 20  
(b) 25  
(c) 10  
(d) None of these
11. When dividing a number X by 30, we get 25 as the quotient and 5 as the remainder. On dividing the same number X by 15, what will be the remainder?
- (a) 0  
(b) 5  
(c) 10  
(d) None of these
12. Each worker, e.g., X, Y, and Z, completes a given task in 5, 10, or 20 hours. If these workers work together, how much time is required in hours to complete a given task?
- (a) Less than 2 hours  
(b)  $35/12$   
(c) 1.5 hours  
(d)  $20/7$

## Part II: Statistics

1. Consider the following data points of a dataset

0, 1, 0, 1, 0,

the mean, median, and mode of the given dataset are

- (a) 0.4, 0 and 0 respectively.  
(b) 0.4, 0 and 1 respectively.  
(c) 0.4, 1 and 0 respectively.  
(d) 0.5, 0 and 0 respectively
2. For a finite value  $n$ , if the standard deviation of the data  $1, 2, \dots, n$  is  $K$ , then the standard deviation of the data  $11, 12, \dots, 10 + n$  is
- (a)  $10K$   
(b)  $K + 10$   
(c)  $K$   
(d)  $K(K + 1) \dots (K + 10)$ .
3. The mean of the following grouped data is

Marks	No. of Students
10-12	6
12-14	8
14-16	5
16-18	7
18-20	4

- (a) 14.67  
(b) 12.54  
(c) 13.67  
(d) 15.27
4. Consider the following dataset What will be the correlation between  $X$  and  $Y$ ?

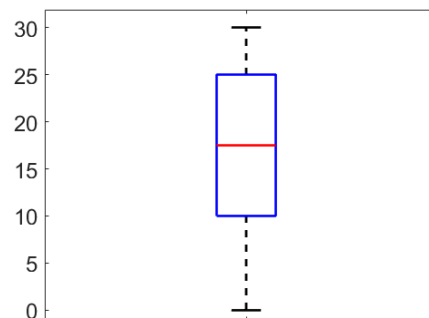
X	Y
1	1
2	1
3	1
4	1
5	1

- (a) 1  
(b) 0.5  
(c) 0  
(d) -1

5. Two cards are drawn randomly from an ordinary deck of 52 cards. Find the probability that both are hearts.

- (a)  $\frac{3}{51}$
- (b)  $\frac{13}{102}$
- (c)  $\frac{2}{13}$
- (d)  $\frac{1}{4}$

6. The inter-quartile range for the dataset represented by the following boxplot is –



- (a) 15
  - (b) 10
  - (c) 25
  - (d) 17.5
7. The expected fraction of data points which lie in the inter-quartile range of the boxplot is
- (a) 0.25
  - (b) 0.60
  - (c) 0.75
  - (d) 0.50
8. For a given continuous random variable  $X$ , let  $F(X)$  be the Cumulative Distribution Function. Consider the following statements :-
- (A)  $F$  should be continuous function.
  - (B)  $F$  should be monotonically non-decreasing function.
  - (C)  $F$  should necessarily be a logarithmic function.

Which group of the above statements is always true ?

- (a) A and B
- (b) B only

- (c) All
- (d) A and C

9. For a given continuous random variable  $X$ , let  $f(X)$  be the density function. Consider the following statements :-

- (A)  $f(x)$  should be always in  $[0,1]$ .
- (B)  $P(a \leq X \leq b)$  can be obtained by evaluating  $\int_a^b f(x)$ .
- (C)  $\int_{-\infty}^{\infty} f(x)$  is 1.

Which group of the above statements is always true ?

- (a) A and C
- (b) B only
- (c) All
- (d) B and C

10. Let  $X$  be a random variable with parameter  $n = 100$  and  $p = 0.2$ , then mean and variance of  $X$  are

- (a) 20 and 16
- (b) 16 and 10
- (c) 20 and 24
- (d) None of above

11. Let  $X$  be the random variable which models the waiting time until an accident at a manufacturing plant and follows the exponential distribution, then for given  $a$  and  $b > 0$ , which of the following is correct ?

- (a)  $P(X > a) = P(X > a + b | X > b)$
- (b)  $P(X > a) > P(X > a + b | X > b)$
- (c)  $P(X > a) < P(X > a + b | X > b)$
- (d) None of above

12. Let the random variable  $X \sim N(\mu, \sigma)$ , then which of them are correct for random variable  $Y = aX + b$  ?

- (a)  $Y \sim N(a\mu + b, a^2\sigma^2)$
- (b)  $Y \sim N(a\mu + b, a^2\sigma + b^2)$
- (c)  $Y \sim N(a^2\mu + b^2, a\sigma^2)$
- (d)  $Y \sim N(a\mu, a\sigma^2)$

## Part III: Mathematics

1. Suppose  $f : [1, 2] \rightarrow \mathbb{R}$  is a continuous function. Then which of the following can be true?

- (a)  $f[1, 2] = (-10, 10000)$ .
- (b)  $f[1, 2] = [-10, 10000)$ .
- (c)  $f[1, 2] = (-10, 10000]$ .
- (d)  $f[1, 2] = [-10, 10000]$ .

2. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a function defined by

$$f(x) = \begin{cases} x^2 \sin(\frac{1}{x}), & \text{if } x \neq 0 \\ 0, & \text{if } x = 0. \end{cases}$$

Then which of the following is true?

- (a)  $f'(0)$  exists and it is equal to 0.
- (b)  $f'(0)$  exists and it is equal to 1.
- (c)  $f'(0)$  does not exist.
- (d)  $f'(0)$  exists and it is equal to 2.

3. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a function defined by

$$f(x) = \begin{cases} \alpha, & \text{if } x < 0 \\ ax^2 - bx + c, & \text{if } x \geq 0. \end{cases}$$

Then  $f$  is continuous at 0 if

- (a)  $\alpha = a$ .
- (b)  $\alpha = b$ .
- (c)  $\alpha = c$ .
- (d) None of the above.

4. Let  $T : M_{n \times n}(\mathbb{R}) \rightarrow M_{n \times n}(\mathbb{R})$  be a linear transformation defined by  $T(A) = A^t$ , where  $A^t$  is the transpose of the matrix  $A$ . Then which of the following is true?

- (a) 0 is an eigenvalue of  $T$ .
- (b) 1 is an eigenvalue of  $T$ .
- (c) 2 is an eigenvalue of  $T$ .
- (d) 3 is an eigenvalue of  $T$ .

5. Which of the following differential equation is exact?

- (a)  $(x^2 + y)dx + (y^2 + x)dy = 0$ .
- (b)  $(x^2 - y)dx + (y^2 + x)dy = 0$ .

- (c)  $(x^2 + y)dx + (y^2 - x)dy = 0$ .
- (d)  $(x + y)^2 dx + (x - y)^2 dy = 0$ .
6. What is the minimum value of the function  $f(x, y) = x^2 + 2y^2 - 2x - 4y$ ?
- (a) 0
- (b) -2
- (c) -1
- (d) -3
7. Let  $f(x, y) = \frac{xy^2}{x^2 + y^4}$ . Then which of the following is true?
- (a)  $\lim_{(x,y) \rightarrow (0,0)} f(x, y) = 0$ .
- (b)  $\lim_{(x,y) \rightarrow (0,0)} f(x, y) = 1$ .
- (c)  $\lim_{(x,y) \rightarrow (0,0)} f(x, y) = -1$ .
- (d)  $\lim_{(x,y) \rightarrow (0,0)} f(x, y)$  does not exist.
8. Suppose  $A$  is a  $100 \times 100$  non-zero matrix with real entries such that  $A^{50} = 0$ . Then which of the following is true?
- (a)  $A$  is invertible.
- (b)  $A$  is diagonalizable.
- (c)  $A^{100} = 0$ .
- (d)  $A$  has a non-zero eigenvalue.
9. Consider the matrix  $M = \begin{pmatrix} 0 & 0 & 0 & 4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$ . Let  $n$  be the number of linearly independent eigen vectors of  $M$ . Then which of the following is true?
- (a)  $n = 1$ .
- (b)  $n = 2$ .
- (c)  $n = 3$ .
- (d)  $n = 4$ .
10. Suppose  $f$  is a continuous function and satisfies the equation  $\int_0^x f(t)dt = x^2 + \sin x$  for all  $x$ . Then what is the value of  $f(\pi/2)$ ?
- (a)  $\frac{\pi}{2}$
- (b)  $\pi$
- (c)  $\frac{\pi}{4}$



(d)  $\frac{\pi^2}{4} + 1$

11. Which of the following is true?

- (a) The series  $\sum_{n=1}^{\infty} \frac{n}{2^n}$  is divergent and the sequence  $\{\frac{1}{\sqrt{n}}\}$  is convergent.
- (b) The series  $\sum_{n=1}^{\infty} \frac{n}{2^n}$  is convergent and the sequence  $\{\frac{1}{\sqrt{n}}\}$  is convergent.
- (c) The series  $\sum_{n=1}^{\infty} \frac{n}{2^n}$  is divergent and the sequence  $\{\frac{1}{\sqrt{n}}\}$  is divergent.
- (d) The series  $\sum_{n=1}^{\infty} \frac{n}{2^n}$  is convergent and the sequence  $\{\frac{1}{\sqrt{n}}\}$  is divergent.

12. Let  $P = \{2, 3, 5, 7, 11, 13, \dots\}$  be the set of prime numbers. Let  $R$  be the radius of convergence of the power series  $f(x) = \sum_{p \in P} x^p$ . Then which of the following is true?

- (a)  $R = 0$ .
- (b)  $R = 1$ .
- (c)  $R = 2$ .
- (d)  $R = 3$ .

## Part IV: Computer Science

1. Which of the following is not a correct example of an Abstract Data Type with respect to the C or C++ programming languages?

- (a) Integer
- (b) Array
- (c) String
- (d) Date

2. Consider the following code snippet for a search algorithm:

```

int CustomeSearch(int a[], int len, int x) {
    int mid, low = 0;
    int high = len - 1;
    while (low <= high) {
        mid = (low+high) / 2;
        if (x == a[mid])
            return mid;
        else if (x > a[mid])
            low = mid+1;
        else
            high = mid-1;
    }
    return -1;
}

```

After  $k^{th}$  iteration, how many elements of the given array will remain alive (i.e., still to be searched)?

- (a)  $\frac{2^k}{n}$
- (b)  $\frac{n}{k}$
- (c)  $\frac{n}{2^k}$
- (d)  $\frac{k}{n}$

3. Consider two strings  $S_1$  and  $S_2$  each having  $k_1$  and  $k_2$  ( $k_1 \leq k_2$ ) characters respectively. Which of the following data structures should you use (in addition to storing  $S_1$  &  $S_2$  themselves) to minimize the worst-case time complexity for counting the unique uncommon characters?

- (a) Auxiliary Queue
- (b) Auxiliary Stack
- (c) Auxiliary 1-D Array
- (d) Auxiliary 2-D Array

4. Suppose an array  $A[-15 \dots 64]$  is stored in a memory. Assume that the word size for each element is 2. How many number of elements are there in the array? Also, if one word of the memory equals 2 bytes, how much memory is required to store the entire array?

- (a) 40, 160 bytes
  - (b) 80, 160 bytes
  - (c) 40, 80 bytes
  - (d) 80, 40 bytes
5. An array is filled with marks of  $k$  students. An algorithm has to be designed for the  $m^{\text{th}}$  highest marks ( $m < k$ ). Select the data structure that would lead to the minimum time-complexity:
- (a) Auxiliary array
  - (b) Auxiliary queue
  - (c) Auxiliary stack
  - (d) No need of additional data structure
6. Which of the following statements is true regarding virtual inheritance in C++?
- (a) It is used to create multiple instances of a base class in a derived class.
  - (b) It resolves the diamond problem by allowing multiple inheritance without creating ambiguity.
  - (c) It is achieved by declaring the base class constructor as virtual.
  - (d) It leads to increased performance due to reduced overhead in managing shared base class instances.
7. Which of the following statements regarding the scope of local variables in C is incorrect?
- (a) Local variables are accessible only within the function in which they are declared.
  - (b) Local variables can be accessed from any function within the same file.
  - (c) Local variables are not accessible outside the block in which they are declared.
  - (d) Local variables may have the same name as global variables without causing conflicts.
8. Which of the following sorting algorithms has a worst-case time complexity of  $O(n^2)$  but a space complexity of  $O(1)$ ?
- (a) Merge Sort
  - (b) Quick Sort
  - (c) Heap Sort
  - (d) Insertion Sort
9. What is the output of the following code snippet?

```
#include <stdio.h>
int main() {
    int x = 5;
    printf("%d", ++x * x++);
    return 0;
}
```

- (a) 30
  - (b) 38
  - (c) 42
  - (d) Compiler Error
10. In C++, which of the following is true regarding the initialization of base class members in a derived class constructor?
- (a) Base class members are automatically initialized by the derived class constructor.
  - (b) Base class members are explicitly initialized using the base class constructor in the member initialization list of the derived class constructor.
  - (c) Base class members are initialized using the derived class constructor body.
  - (d) Base class members are initialized using the default constructor of the base class.

11. What is the output of the following code snippet?

```
#include <stdio.h>
void foo(int x) {
    printf("%d ", x);
    if (x > 0)
        foo(--x - 1);
}
int main() {
    foo(3);
    return 0;
}
```

- (a) 3 2 1 -1
  - (b) 0 1 2 3
  - (c) 3 1 0
  - (d) 3 1 -1
12. Consider a 2D Array filled up with marks and roll numbers of  $N$  students. If the marks can range from  $0 : m$  then what will be the **best-case** space complexity of storing the marks.
- (a)  $\Omega(mN)$
  - (b)  $\Omega(m + N)$
  - (c)  $\Omega(m^2)$
  - (d)  $\Omega(N^2)$